Timing is Money:
The Value of Execution Scheduling

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Liquid Markets Analytics
The Troika of Quantitative Investment

- Primary focus of the quant community
- Factor models to exploit behavioural biases in security valuation
- Represent systematization of the stock selection process

- Focus on loss preservation and efficient capital allocation
- Estimated using fundamental/statistical factor models
- Generally purview of third-party vendors but recently an area of internal focus

- Measures shortfall due to the implementation process
- Depends critically on the execution style and strategy (front-loaded, passive, back-loaded, etc)
- Usually receives the least focus by quants
Trade Implementation as a Scientific Process

- Market impact modeling
  - Model estimation principles similar to multi-factor modeling in alpha research
  - Markets have memory so static impact models are not adequate
  - Example: Nomura METRIC model

- Liquidity, volume profile and volatility prediction
  - PCA decomposition of volume into systematic and idiosyncratic components
  - Estimating volatility using non-stationary and non-synchronous tick data
  - Example: Nomura Volume Prediction and Volatility Prediction Models

- Optimal trade scheduling
  - Non-linear optimization techniques similar to multi-period portfolio construction
  - Example: Nomura Portfolio Target Strike Algorithm
Including Execution Costs in the Investment Process

- Traditional portfolio construction paradigm
  - Construct optimal portfolio by balancing alpha and risk
  - Well-understood problem since the 70s
  - Transaction costs estimates used for post-facto filtering (pre-trade)
  - Sub-optimal since transaction costs are not included “upstream”

- Modern portfolio construction paradigm:
  - Construct optimal portfolio by balancing alpha, risk and execution cost
  - Complex problem since transaction costs depend on both the alpha and the trading process
  - Allows optimal allocation of capital across different tradable opportunities
Execution Algorithms Systematize Implementation

- Execution algorithms implement a systematic trade implementation process
  - Process vast amount of real-time market data
  - Make simultaneous trading decisions at different time scales

- Execution algorithms can be decomposed into three modules
  - Trade scheduling algorithm slices the original institutional size order into a sequence of smaller trades (minutely horizon decisions)
  - Order placement algorithm decides type and timing of trades to send to the market (secondly horizon decisions)
  - Market access algorithm decides which destination to route each order (millisecond horizon decisions)
Construction of Trade Scheduling Algorithms

- Trade Scheduling Algorithms are typically formulated as optimization problems.

- Price evolution model: Random walk, Short-term momentum, Mean-reversion
- Market impact model: Instantaneous, with Memory
- Performance criteria – deviation from a target benchmark
- Trade as quickly as possible to reduce opportunity cost without causing market impact
Examples of Trade Scheduling Algorithms

- **Static Trade Scheduling Algorithms**
  - Optimization to compute trade schedule is performed initially
  - Computed trade schedule is kept constant throughout trading interval (e.g., VWAP, TWAP)

- **Dynamic Trade Scheduling Algorithms**
  - Trade schedule is re-optimized at the beginning of each bin
  - Optimization criterion is fixed but depends on market conditions (e.g., Participation, Dynamic VWAP)

- **Adaptive Trade Scheduling Algorithms**
  - Trade schedule is re-optimized at the beginning of each bin
  - Optimization criterion changes in response to market condition (e.g., Aggressive/Passive In The Money)
Measuring Performance of Execution Algorithms

- Execution cost is measured as the difference between execution price and the benchmark
  - estimated pre-trade
  - measured post-trade
  
  \[
  \text{ExecutionCost} = \text{ExecPrice} - \text{BenchmarkPrice} = \text{OrderPlacementCost} + \text{TradeSchedulingCost}
  \]

- There is no universal execution benchmark
  - Arrival price: used by quant funds
  - Close price: used by index and mutual funds
  - VWAP price: used as execution benchmark large multi-day trades (e.g., buyback)

Source: Nomura Securities International, Inc.
VWAP

- Trade proportionally to the historical volume profile
  - Reduces standard deviation of the trade scheduling cost
  - Reduces mean of the order placement cost
  - Performs well when price evolves as a random walk and price and volume are uncorrelated

- Exchange specific historical volume profiles
- Stock specific historical volume profile

Source: Nomura Securities International, Inc.
Dynamic VWAP

- Trade proportionally to the estimated volume profile
  - Volume profile is estimated in each bin based on the volume profile prior to this bin
  - Attempts to reduce standard deviation of the trade scheduling cost and improve mean of the order placement cost

Snapshot of the Realized/Estimated volume profile

Source: Nomura Securities International, Inc.
Aggressive/Passive in the Money

- Trade depending on the price evolution
  - Attempts to reduce the mean scheduling cost at the expense of standard deviation

- Passive-in-the-Money (PIM): performs well when price exhibits momentum
  - Accelerate if the price moves unfavorably
  - Decelerate if the price moves favorably

- Aggressive-in-the-Money (AIM): performs well when price exhibits mean-reversion
  - Decelerate if the price moves favorably
  - Decelerate if the price moves unfavorably

Source: Nomura Securities International, Inc.
Simulation Framework

- Goals
  - Compare performance of different trade scheduling algorithms
  - Infer properties of recent markets

- Data set consists of actual orders received by Nomura’s PT desk
  - Full day orders from Jan to May 2009 (approx. 15,000)

- Individual bin execution price is assumed to occur at local VWAP

- Price movement during the day
  - 10 bps for buy orders
  - 20 bps for sell orders
  - Price “trends” between 2pm and close

Source: Nomura Securities International, Inc.
## VWAP Results

<table>
<thead>
<tr>
<th></th>
<th>Sell</th>
<th></th>
<th>Buy</th>
<th></th>
<th>Total</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mean (bps)</td>
<td>std (bps)</td>
<td>mean (bps)</td>
<td>std (bps)</td>
<td>mean (bps)</td>
<td>std (bps)</td>
</tr>
<tr>
<td>Exchange historical profile</td>
<td>-2.8</td>
<td>28.2</td>
<td>2.7</td>
<td>23.7</td>
<td>0.2</td>
<td>26.0</td>
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<tr>
<td>Stock historical profile</td>
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<td>27.2</td>
<td>0.8</td>
<td>22.8</td>
<td>0.3</td>
<td>25.2</td>
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<tr>
<td>Dynamic VWAP</td>
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<td>24.5</td>
<td>1.5</td>
<td>23.1</td>
<td>-0.2</td>
<td>23.8</td>
</tr>
</tbody>
</table>

Source: Nomura Securities International, Inc.

- **Stock historical profiles outperform exchange specific profiles**
  - Improves overall performance
  - Reduces magnitude of the mean trade scheduling costs as a function of the trading direction
  - Reduces standard deviation of the trade scheduling cost

- **Dynamic VWAP**
  - Reduces standard deviation of the trade scheduling cost
  - Degrades overall mean trade scheduling cost
  - Improves mean trade scheduling cost for buys and degrades it for sells
PIM/AIM Results

- PIM dramatically improves mean cost for sell trades
  - Price predominantly evolves as a momentum process

- Adaptation does not materially improve mean cost for buy trades
  - Price predominantly evolves as a random-walk

- Adaptation increases standard deviation of the trade scheduling cost
  - Stronger the adaptation, the larger standard deviation

Source: Nomura Securities International, Inc.
Dynamic PIM/AIM Results

- Detecting market regime
  - Large price move indicates momentum
  - Small price move indicates mean-reversion
- Estimating the market regime dramatically reduces cost
- Can market regime be estimated?

<table>
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</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mean (bps)</td>
<td>std (bps)</td>
<td>mean (bps)</td>
</tr>
<tr>
<td><strong>Dynamic AIM/PIM</strong></td>
<td>0.1</td>
<td>58.8</td>
<td>-0.2</td>
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</tbody>
</table>

Source: Nomura Securities International, Inc.
Conclusion

- Execution cost is an important determinant of investment performance
  - Execution cost can be modeled and controlled using scientific methods
  - Can be decomposed into order placement and trade scheduling components

- Trade scheduling algorithm fundamentally impacts trade implementation
  - Knowledge of current market regime can significantly reduce the execution cost
  - Novel algorithms for market regime detection and liquidity estimation are needed
  - Timing is money!
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